## GCSE Mathematics

## Practice Tests: Set 24

## Paper 2H/3H (Calculator)

## Time: 1 hour 30 minutes

You should have: Ruler graduated in centimetres and millimetres, protractor, pair of compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.

## Instructions

- Use black ink or ball-point pen.
- Fill in the boxes at the top of this page with your name, centre number and candidate number.
- Answer all questions.
- Answer the questions in the spaces provided - there may be more space than you need.
- Calculators may be used.

- Diagrams are NOT accurately drawn, unless otherwise indicated.
- You must show all your working out.


## Information

- The total mark for this paper is 80
- Questions are in order of mean difficulty as found by students achieving Grade 7.
- The marks for each question are shown in brackets
- use this as a guide as to how much time to spend on each question.


## Advice

- Read each question carefully before you start to answer it.
- Keep an eye on the time.
- Try to answer every question.
- Check your answers if you have time at the end.


## Answer ALL TWENTY ONE questions.

Write your answers in the spaces provided.
You must write down all the stages in your working.

160 students sat a Mathematics exam.
The mean mark for the 32 students in Class A was 55
The mean mark for the 28 students in Class B was 52

Find the mean mark for all 60 students.

2 Teresa invests $£ 2000$ for 3 years in a savings account. She gets $4 \%$ each year compound interest.
(a) How much money will Teresa have in her savings account at the end of 3 years? Give your answer correct to the nearest pound.
$\qquad$

Sam invested $£ T$
The value of his investment decreased by $9 \%$ each year.
At the end of the first year, the value of Sam’s investment was $£ 1365$
(b) Work out the value of $T$

3 Divya and Yuan each pay for a holiday at a special offer price.

| Divya's holiday |
| :---: |
| Normal price: $\$ 1600$ |
| Special offer: |
| $16 \%$ off the normal price |

Yuan's holiday<br>Normal price: $\$ 1400$<br>Special offer:<br>$k \%$ off the normal price

The amount that Divya pays is the same as the amount that Yuan pays.
Work out the value of $k$

$$
k=.
$$



Diagram NOT accurately drawn

Solid $\mathbf{A}$ is in the shape of a cylinder with radius 3 cm and height 7 cm Solid A has a mass of 2000 g
Solid B has a mass of 3375 g
Solid B has a volume of $450 \mathrm{~cm}^{3}$
All of the metal from Solid $\mathbf{A}$ and $\operatorname{Solid} \mathbf{B}$ is melted down to make a uniform Solid $\mathbf{C}$
Given that there is no change to mass or volume during this process work out the density of Solid C

Give your answer correct to one decimal place.
$\mathrm{g} / \mathrm{cm}^{3}$

$$
\begin{aligned}
& A=2^{3} \times 3 \times 5 \times 7^{2} \\
& B=2 \times 3^{2} \times 7 \\
& C=3 \times 5^{2} \times 11
\end{aligned}
$$

(b) Find the lowest common multiple (LCM) of $A, B$ and $C$

Write your answer as a product of powers of prime factors.
$6 \quad C$ grams of chocolate is shared in the ratios 2:5:8
The difference between the largest share and the smallest share is 390 grams.
Work out the value of $C$

$$
C=
$$

(Total for Question 6 is $\mathbf{3}$ marks)

7 The table shows information about the frame size, in cm , of 60 bicycles sold in a shop.

| Frame size ( $\boldsymbol{S} \mathbf{~ c m})$ | Frequency |
| :---: | :---: |
| $30<S \leq 36$ | 4 |
| $36<S \leq 42$ | 14 |
| $42<S \leq 48$ | 18 |
| $48<S \leq 54$ | 19 |
| $54<S \leq 60$ | 5 |

(a) Write down the modal class.
(b) Work out an estimate for the mean frame size.
cm

8 In a bag, there are only red counters, blue counters, green counters and yellow counters.
The total number of counters in the bag is 80
In the bag
the number of red counters is $x+7$
the number of blue counters is $x-11$
the number of green counters is $3 x$
Jude takes at random a counter from the bag.
The probability that he takes a red counter is $\frac{1}{4}$
Work out the probability that Jude takes a yellow counter.

9 The diagram shows a solid triangular prism.


Diagram NOT accurately drawn

Work out the total surface area of the triangular prism.
Give your answer correct to 3 significant figures.
$\mathrm{cm}^{2}$

10 The diagram shows an isosceles triangle $A B C$


Diagram NOT accurately drawn
$A B=7 \mathrm{~cm} A C=B C=y \mathrm{~cm}$
The area of the triangle is $42 \mathrm{~cm}^{2}$
Work out the value of $y$

$$
y=
$$

11 The table shows information about the times, in minutes, that 80 patients had to wait to see a doctor.

| Time ( $W$ minutes) | Frequency |
| :---: | :---: |
| $0<W \leq 10$ | 7 |
| $10<W \leq 20$ | 10 |
| $20<W \leq 30$ | 15 |
| $30<W \leq 40$ | 32 |
| $40<W \leq 50$ | 16 |

(a) Complete the cumulative frequency table below.

| Time ( $W$ minutes) | Cumulative <br> frequency |
| :---: | :---: |
| $0<W \leq 10$ |  |
| $0<W \leq 20$ |  |
| $0<W \leq 30$ |  |
| $0<W \leq 40$ |  |
| $0<W \leq 50$ |  |

(b) On the grid on the next page, draw a cumulative frequency graph for your table.

(c) Use your graph to find an estimate for the median.
$\qquad$ minutes
(1)
(d) Use your graph to find an estimate for the interquartile range.
$\qquad$
$12 \quad T=\frac{p}{r}$
$p=0.51$ correct to 2 significant figures.
$r=6.3$ correct to 2 significant figures.
Work out the upper bound for the value of $T$
Show your working clearly.

13 Using ruler and compasses only, construct the bisector of angle $B A C$ You must show all your construction lines.


$A B, B C, C D, D E$ and $E F$ are five sides of a regular polygon.
RST, SCU and BCV are straight lines.
$R S T$ is parallel to $C D$
Angle $R S C=128^{\circ}$
Angle $U C V=32^{\circ}$
Work out how many sides the polygon has.
Show your working clearly.

15 The diagram shows a triangular prism, $A B C D E F$, with a rectangular base $A B C D$


## Diagram NOT

 accurately drawn$A B=6 \mathrm{~cm}$
$D E=2.2 \mathrm{~cm}$ angle
$D A E=18^{\circ}$
angle $A D E=90^{\circ}$
Work out the angle that $B E$ makes with the plane $A B C D$ Give your answer correct to one decimal place.

16 A rectangle has length $L$ and width $W$
$L$ is increased by $20 \%$
$W$ is decreased by $35 \%$
Calculate the percentage reduction in the area of the rectangle.
.


Diagram NOT accurately drawn
$A B=4.6 \mathrm{~cm} \quad B C=8.3 \mathrm{~cm} \quad$ angle $A B C$ is acute
The area of triangle $A B C$ is $12 \mathrm{~cm}^{2}$
Work out the perimeter of triangle $A B C$
Give your answer correct to 3 significant figures.
cm

18 The table gives information about the time taken by each student in Year 11 to complete a homework task.

| Time taken $(t$ minutes $)$ | Frequency |
| :---: | :---: |
| $10<t \leq 25$ | 15 |
| $25<t \leq 30$ | 18 |
| $30<t \leq 50$ | 32 |
| $50<t \leq 60$ | 4 |

(a) On the grid, draw a histogram for this information.


One of these students who took 50 minutes or less and more than 25 minutes to complete this homework task is chosen at random.
(b) Find an estimate for the probability that this student took 45 minutes or less to complete this homework task.

19 A statue and a model of the statue are mathematically similar.
The statue has a total surface area of $3600 \mathrm{~cm}^{2}$
The model has a total surface area of $625 \mathrm{~cm}^{2}$
The volume of the model is $750 \mathrm{~cm}^{3}$
Work out the volume of the statue.
$\mathrm{cm}^{3}$

20 Here are the numbers of aces that Rutger served in each of 11 tennis matches.
$\begin{array}{lllllllllll}1 & 1 & 2 & 4 & 6 & 8 & 8 & 9 & 11 & 12 & 15\end{array}$
(a) Find the interquartile range of the numbers of aces.

Show your working clearly.
$\qquad$

Kim also plays in 11 tennis matches.

## For Kim

the median number of aces is 11
the interquartile range of the numbers of aces is 5
(b) State, giving a reason, whether Rutger or Kim
(i) served more aces on average,
$\qquad$
$\qquad$
$\qquad$
(ii) was more consistent with the number of aces served.
$\qquad$
$\qquad$
$\qquad$


Diagram NOT accurately drawn

The radius of the circle is 8.5 cm
Angle $A B C=132^{\circ}$
Work out the perimeter of the shaded sector $A O C$
Give your answer correct to 3 significant figures.

